Data Structures and Algor nal Linguistics III (IGCL-RA-07)

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A tree is a set of nodes organ hierarchically with the follow

Definitions

Ordered trees

or If a tree is non-empty, it has a special node called root node Except the root node, every node in the tree has a unique parent (all nodes except the root are children of another node)

Alternatively, we can define a tre-recursively:

The empty set of nodes is a tree
 Otherwise a tree contains a roo
 with sub-trees as its children



A tree is ordered if there is an ordering between siblings. Typical examples include:

A tree representing a document (e.g., HTML) structure
 Parse trees
 (maybe) a family tree

. In many cases order is not important

Class hierarchy in a object-oriented prog
 The tree representing files in a computer

Some properties of binary trees

For a binary tree with  $n_g$  leaf,  $n_1$  internal, nnodes and with height h

•  $h+1 \leqslant n \leqslant 2^{h+1}-1$ 

 $\bullet\ h\leqslant n_i\leqslant 2^h-1$  $\bullet \ 1\leqslant n_{g}\leqslant 2^{h}$ 

•  $log(n+1)-1 \leqslant h \leqslant n-1$ • For any proper binary tree,  $n_{\ell} = n_{\perp} + 1$ 



Implementation of trees





Breadth first traversal (level order)



queue append(root)
while queue:
node = queue.pop(0)
# process the node
print(node.data)
for child in node.children:
queue.append(child)

Why study trees

. A tree is a hierarchical non-linear data structure useful in n  $\ast$  We have already resorted to descriptions using trees (e.g., recursion trace)

A Tree is a graph with certain properties
It is also very common in (computational) linguistics:
Pare these representing syntactic structure of sentences
Language trees: representing the historical relations between languages
Decision trees a well-known algorithm for machine learning, also used for many NLT problems

More definitions

## \* The nodes with the same parent are called siblings The nodes with children are called internal nodes

. The nodes without children are the leaf nodes

· A path is a sequence of connected nodes Any node in the path from the root to a particular node is its ancestors

. A node is a descendant of its ancestors \* A subtree is a tree rooted by a non-root node

The depth of a node is the number of edges from root
 The height of a node is the number of edges from the

. The height of a tree is the height of its root

## Binary trees

. Binary trees where nodes can have at most two children, have many applications Binary trees have a natural order, each child is either

a left child or a right child A binary tree is proper, or full if every node has either

two children or none In a complete binary tree, every level except possibly the last, is completely filled, and all nodes at the last level is at the left

A perfect binary tree is a full binary tree whose leaf nodes have the same depth

Binary tree example: expression trees

# Implementation of trees

. Binary trees can also be implemented with arrays

the root node is stored at index 0
the left child of the node at index 1 is stored at 2i + 1
the right child of the node at index i is stored at 2i + 2
the parent of the node at index i is stored at 2i + 2
the parent of the node at index i is at index [[i - 1]/2]

. If the binary tree is complete, this representation



## Pre-order traversal



def pre\_order(node)

print(node.data) for child in node.children: pre\_order(child)

