

## Transforming one string to another

- The table (back arrows) also gives a set of edit operations to trastring to another
- For LCS, operations are
  - copy (diagonal arrows in the details)
- insert (left arrows in the demo assuming original string is the vertical one)
  delete (up arrows in the demo) These also form an alignment between two strings
- · Different set of edit operations recovered will yield the same LCS, but different alignments

## LCS alignments

		0	1	2	3	4	5	6	7	8	
		¢	h	1	у	8	e	1	n	e	
0	c	0	0	0	0	0	0	0	0	0	Alignments
1	h	0	1+	-1	1	1	1	1	1	1	h-yg-ione
2	у	0	1	1	2	2	2	2	2	2	ciccicicc hiygei-me
3	8	0	1	1	2	3.	-3	3	3	3	h-ygie-ne
4	1	0	1	2	2	3	3	4	4	4	ciccócico
5	c	0	1	2	2	3	4+	-4	4	5	hiyg-eine
6	n	0	1	2	2	3	4	4	5	5	
7	c	0	1	2	2	3	4	4	5	6	

#### LCS - some remarks

- + We formulated the algorithm as maximizing the LCS
- + Alternatively, we can minimize the costs associated with each operation: - copy = 0 - delete = - insert =
- + The cost settings above are the typical, e.g., as in diff
- In some applications we may want to have different costs for delete and ins (e.g., mapping lemmas to inflected forms of words)
- Similarly, we may want to assign different costs for differ higher cost to delete consonants in historical linguistics) nt characters (e.g.



### Edit distance: extensions and variations

- · Another possible operation we did not cover is some (or transpose), which is useful for applications like spell checking
- + In some applications (e.g., machine translation, OCR correction) we may
- want to have one-to-many or many-to-one alignments
- Additional requirements often introduce additional complexity
- · It is sometimes useful to learn costs from data

Acknowledgments, credits, references

- Goodrich, Michael T., Roberto Tamassia, and Michael H. Goldwasser (2013). Data Structures and Algorithms in Python. John Wiley & Sons, Incorporated. so
- Data Structures and acquirement of generative systems of the system o

if len(Yy) = 0

if len(Xx) = 0

if x = y

# Levenshtein distance

- · Levenshtein difference between two strings is the total cost of inserti deletions and substitut
- · With cost of 1 for all operations

 $\int len(X)$ len(Y)  $lev(Xx,Yy) = \begin{cases} lev(X,Y) \end{cases}$  $1 + \min \begin{cases} lev(X, Yy) \\ lev(Xx, Y) \\ lev(X, Y) \end{cases}$ 

· Naive recursion (as defined above), again, is intractable

+ But, the same dynamic programming method works

Levenshtein distance

		0	1	2	3	4	5	6	7	8
		c	h	1	у	8	е	1	n	е
0	c	0	1	2	3	4	5	6	7	8
1	h	1	0+	-1	2	3	4	5	6	7
2	у	2	1	1	1	2	3	4	5	6
3	8	3	2	2	2	1.	-2	3	4	5
4	1	4	3	2	3	2	2	2	3	4
5	с	5	4	3	3	3	2+	Ч.	3	3
6	n	6	5	4	4	4	3	3	3	4
7	e	7	6	5	5	5	4	4	4	3

### Summary

- + Edit distance is an important problem in many fields including computational linguistics
- A number of related problems can be efficiently solved by dyn
- programming Edit distance is also important for approximate string matching and alignr
- Reading suggestion: Goodrich, Tamassia, and Goldwasser (2013, chapter 13), Jurašsky and Martin (2009, section 3.11, or 2.5 in online draft)
- Next

· Algorithms on strings: tries

· Reading: Goodrich, Tamassia, and Goldwasser (2013, chapter 13),

