

# Top-down Chart Parsing: the Earley algorithm

## Data Structures and Algorithms for Computational Linguistics III (ISCL-BA-07)

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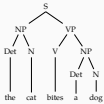
## Parsing so far

- We can formulate parsing as
  - Top-down: begin with the start symbol, try to *produce* the input string to be parsed
  - Bottom-up: begin with the input, and try to *reduce* it to the start symbol
- Another aspect of a parser is its *directionality*. Two choices are:
  - Directional: parses processes the input left to right (right to left is also possible, but rarely used)
  - Non-directional: order is not important, typically require all input to be in memory before processing

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## Top-down parsing as search



S → NP VP  
NP → Det N  
VP → V NP  
VP → V  
Det → a  
Det → the  
N → cat  
N → dog  
V → bites

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## Earley algorithm

- Earley algorithm is a top down (and left-to-right) parsing algorithm
- It allows arbitrary CFGs
- Keeps record of constituents that are predicted using the grammar (top-down) in-progress with partial evidence completed based on input seen so far at every position in the input string
- Time complexity is  $O(n^3)$

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## Earley chart entries (states or items)

Earley chart entries are CF rules with a 'dot' on the RHS representing the state of the rule

- $A \rightarrow \alpha \bullet \beta[i, i]$  predicted without any evidence (yet)
- $A \rightarrow \alpha \bullet \beta[i, j]$  partially matched
- $A \rightarrow \alpha \beta \bullet [i, j]$  completed, the non-terminal  $A$  is found in the given span

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## Earley algorithm: an informal sketch

1. Start at position 0, predict  $S$
2. Predict all possible states (rules that apply)
3. Read a word
4. Update the table, advance the dot if possible
5. Go to step 2
6. If we have a completed  $S$  production at the end of the input, the input is recognized

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## Earley algorithm: three operations

**Predictor** adds all rules that are possible at the given state

**Completer** adds states from the earlier chart entries that match the completed state to the chart entry being processed, and advances their dot

**Scanner** adds a completed state to the next chart entry if the current category is a pre-terminal symbol, and the terminal symbol (word) matches

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## Earley parsing example (chart[0])

0	she	1	saw	2	a	3	duck	4
state	rule	position	operation					
0	$\gamma \rightarrow \bullet S$	[0,0]	initialization					
1	$S \rightarrow \bullet NP VP$	[0,0]	predictor					
2	$S \rightarrow \bullet Aux NP VP$	[0,0]	predictor					
3	$NP \rightarrow \bullet Det N$	[0,0]	predictor					
4	$NP \rightarrow \bullet NP PP$	[0,0]	predictor					
5	$NP \rightarrow \bullet Prn$	[0,0]	predictor					

Note: the chart[0] is independent of the input.

S → NP VP  
S → Aux NP VP  
NP → Det N  
NP → Prn  
NP → NP PP  
VP → V NP  
VP → V  
PP → V PP  
PP → Prp NP  
N → duck  
N → park  
V → duck  
V → saw  
Prn → she | her  
Prp → in | with  
Det → a | the  
Aux → does | has

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## Earley parsing example (chart[1])

0	she	1	saw	2	a	3	duck	4
state	rule	position	operation					
6	$Prn \rightarrow she \bullet$	[0,1]	scanner					
7	$NP \rightarrow Prn \bullet$	[0,1]	completer					
8	$S \rightarrow NP \bullet VP$	[0,1]	completer					
9	$NP \rightarrow NP \bullet PP$	[0,1]	completer					
10	$VP \rightarrow \bullet V NP$	[1,1]	predictor					
11	$VP \rightarrow \bullet V$	[1,1]	predictor					
12	$VP \rightarrow \bullet VP PP$	[1,1]	predictor					
13	$PP \rightarrow \bullet Prp NP$	[1,1]	predictor					

S → NP VP  
S → Aux NP VP  
NP → Det N  
NP → Prn  
NP → NP PP  
VP → V NP  
VP → V  
PP → V PP  
PP → Prp NP  
N → duck  
N → park  
V → duck  
V → saw  
Prn → she | her  
Prp → in | with  
Det → a | the  
Aux → does | has

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## Earley parsing example (chart[2])

0	she	1	saw	2	a	3	duck	4
state	rule	position	operation					
14	$V \rightarrow saw \bullet$	[1,2]	scanner					
15	$VP \rightarrow V \bullet NP$	[1,2]	completer					
16	$VP \rightarrow V \bullet$	[1,2]	completer					
17	$S \rightarrow NP VP \bullet$	[0,2]	completer					
18	$NP \rightarrow \bullet Det N$	[2,2]	predictor					
19	$NP \rightarrow \bullet NP PP$	[2,2]	predictor					
20	$NP \rightarrow \bullet Prn$	[2,2]	predictor					

S → NP VP  
S → Aux NP VP  
NP → Det N  
NP → Prn  
NP → NP PP  
VP → V NP  
VP → V  
PP → V PP  
PP → Prp NP  
N → duck  
N → park  
V → duck  
V → saw  
Prn → she | her  
Prp → in | with  
Det → a | the  
Aux → does | has

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## Earley parsing example (chart[3])

0	she	1	saw	2	a	3	duck	4
state	rule	position	operation					
21	$Det \rightarrow a \bullet$	[2,3]	scanner					
22	$NP \rightarrow Det \bullet N$	[2,3]	completer					

S → NP VP  
S → Aux NP VP  
NP → Det N  
NP → Prn  
NP → NP PP  
VP → V NP  
VP → V  
PP → V PP  
PP → Prp NP  
N → duck  
N → park  
V → duck  
V → saw  
Prn → she | her  
Prp → in | with  
Det → a | the  
Aux → does | has

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## Earley parsing example (chart[4])

0	she	1	saw	2	a	3	duck	4
state	rule	position	operation					
23	$N \rightarrow duck \bullet$	[3,4]	scanner					
24	$V \rightarrow duck \bullet$	[3,4]	scanner					
25	$NP \rightarrow Det N \bullet$	[2,4]	completer					
26	$VP \rightarrow V NP \bullet$	[1,4]	completer					
27	$S \rightarrow NP VP \bullet$	[0,4]	completer					

S → NP VP  
S → Aux NP VP  
NP → Det N  
NP → Prn  
NP → NP PP  
VP → V NP  
VP → V  
PP → V PP  
PP → Prp NP  
N → duck  
N → park  
V → duck  
V → saw  
Prn → she | her  
Prp → in | with  
Det → a | the  
Aux → does | has

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Earley parsing: summary

- Complexity (asymptotic) is the same as CKY
  - time complexity :  $O(n^3)$
  - space complexity:  $O(n^2)$
- Our example shows recognition, we need to maintain back links for parsing
- Again, the Earley chart stores a parse forest compactly, but extracting all trees may require exponential time

Summary

- The Earley parser is a top-down parser with bottom-up filtering (or, you can also view it the other way around)
- The parser improves over a backtracking parser by
  - dynamic programming: not re-computing the subtrees
  - filtering: not generating hypotheses (predictor) that cannot match at a given input position
- It can process any CFG (no need for CNF)
- There is a nice relation between CKY and Earley: you can view Earley as binarizing the grammar (converting to CNF) ‘on the fly’
- Suggested reading: [grune2008](#)

Next:

- Dependency parsing
- Reading suggestion: [jurafsky2009](#)

An exercise

Construct the CKY and Earley charts for the sentence below

The duck she saw is in the park

Recommended grammar:

S	→	NP VP	PP	→	Prp NP
NP	→	Det N	N	→	park
NP	→	Prn	N	→	duck
NP	→	NP PP	V	→	is
NP	→	NP S	V	→	saw
VP	→	V NP	Prn	→	she
VP	→	V	Prp	→	in
VP	→	VP PP	Det	→	the

Acknowledgments, references, additional reading material